

## Modeling of photonic band gap in two dimensional photonic crystals made by sol gel process

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**Abstract:** Photonic band gap of two dimensional photonic crystals fabricated by  $\text{SiO}_2/\text{ZrO}_2$  or  $\text{SiO}_2/\text{TiO}_2$  with sol-gel process in which the refractive index varied in the range of 1.51 to 1.57 has been investigated in the present paper. The structure studied consists of circular air holes of radius  $r$  embedded in matrix, while  $a$  is the constant of triangular lattice. Finite difference time domain method (FDTD) with perfectly matched layers (PML) was used to calculate the transmission spectrum by FullWAVE software. The results of simulation clearly demonstrate the existence of photonic band gap of which the position and the width are strongly affected by refractive index. In the other hand, the effects of geometric parameters (air hole radius  $r$  and lattice period  $a$ ) on the photonic band gap have been investigated in this work.

**Key words:** 2D photonic crystals, low contrast, FDTD, photonic band gap, sol-gel process.

### Introduction

Photonic crystals (PhCs) are artificial materials in which the dielectric constant  $\epsilon$  (the refractive index  $n$ ) has a periodicity in one, two or three dimensions. They are called one-dimensional (1D), two-dimensional (2D) and three-dimensional (3D) photonic crystals respectively. Since the introduction of the concept of photonic crystals by E. Yablonovich [1] and S. John [2], they have attracted much interest due to their potential for controlling the propagation of light for its photonic band gap (PBG) and/or light diffraction properties [3-4].

In recent years, 2D (PhCs) composed of air holes drilled in a dielectric slab and structured in a triangular lattice are most commonly used due to the difficulty in the fabrication of other types of photonic crystals (3D). In the other hand, 2D photonic crystals have a great ability for integration [3]. Consequently, they have been widely studied and analyzed as the building blocks to realize functional devices for optical networking [3], waveguides [5-6], photonic crystal fibers [7], photonic cavities [8-9], and optoelectronics applications. Generally, in the optical and near-IR regions of the spectrum it is important to start with computational and modeling of design and properties before the fabrication processes because photonic crystals are expensive. In the first part of this work, we have demonstrated the existence of photonic band gap in 2D photonic crystals fabricated with  $\text{SiO}_2/\text{ZrO}_2$  or

$\text{SiO}_2/\text{TiO}_2$  made by sol-gel process [10], this later is characterized with low refractive index which varied in the range of 1.51 to 1.57 at  $\lambda=1.55\mu\text{m}$  [11]. In the second part, we have investigated the effects of the contrast and the geometrical parameters (lattice period and air hole radius) on the photonic band gap variations.

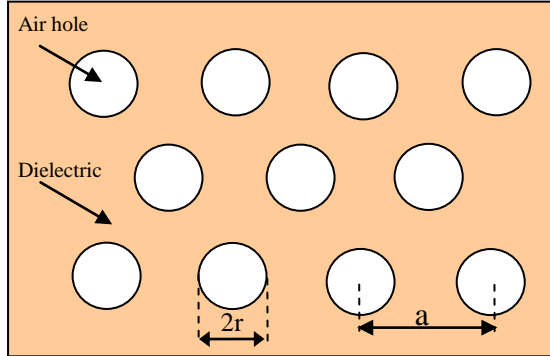
Fullwave is a simulation engine which calculates the electromagnetic field as a function of time and space in a given index structure in response to a given electromagnetic excitation. Fullwave is ideal for studying the propagation of light in a wide variety of photonic structures. In this work, the simulation engine is based on the well-known finite difference time domain method (FDTD) with perfectly matched layers (PML) in order to calculate the transmission spectrum [12].

### I. Structure

The 2D photonic crystal to be studied and analyzed in the present paper consists of  $33 \times 33$  array of circular air holes of radius  $r=0.27\mu\text{m}$  which are structured in triangular lattice of period  $a=0.75\mu\text{m}$ . However, the triangular lattice is very suitable to studying photonic band gap properties. The triangular lattice allows the opening of 2D photonic band gap, presents a good compromise namely for high filling factors and it's

lowly sensitive to the incidence angle compared to the square lattice [13-14].

The studied structure is showed in Figure 1, where the air holes ( $n=1$ ) are embedded in a  $\text{SiO}_2/\text{ZrO}_2$  or  $\text{SiO}_2/\text{TiO}_2$  dielectric. The later is characterized by the background index varying in the range of 1.51 to 1.57.



**Fig.1. Connected structure of 2D photonic crystal made with air holes in dielectric.**

In this study, the triangular lattice was created using the array layout XZ utility. The different results of transmission spectrum obtained show that 2D photonic crystal characterized with low contrast present a photonic band gap only for TM polarization (transverse magnetic) and no band for TE polarization (transverse electric).

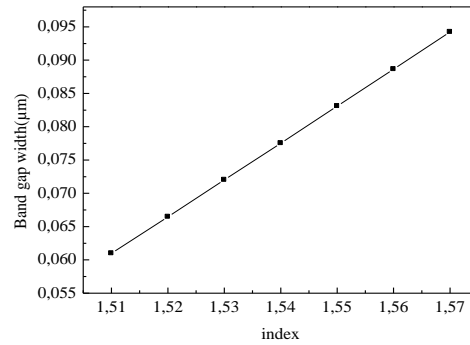
## II. Effect of refractive index

In this section, we will discuss the conditions of opening a photonic band gap in 2D photonic crystals described in previous section and the variations of its position and size as a function of refractive index.

The simulations are based on the well known finite-difference time-domain (FDTD) technique. Firstly, before any simulation we are fixed geometrical parameters ( $a=0.75\mu\text{m}$  and  $r=0.27\mu\text{m}$ ). After that, we calculated photonic band gap width for each value of refractive index. All results demonstrate clearly the existence of TM band gap.

Figure 2 shows the effect of refractive index on the width of the photonic band gap characterized with feeling factor  $r/a=0.36$ . Furthermore, from results we can conclude that the width of photonic band gap is strongly influenced by refractive index. The width  $\Delta\lambda$  ( $\mu\text{m}$ ) was increased from  $\Delta\lambda=0.0609\mu\text{m}$ , for low index ( $n=1.51$ ), to  $\Delta\lambda=0.0942\mu\text{m}$ , for high index ( $n=1.57$ ). Either the largest band gap, the high refractive index it is. Which agree with other studies concerning other materials [15-16].

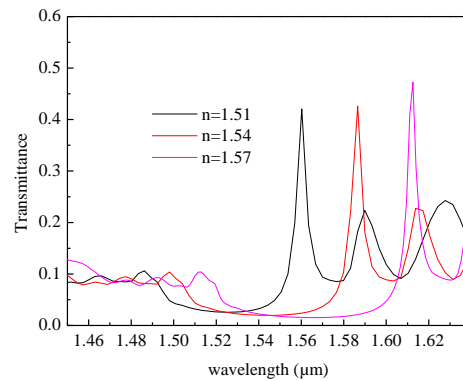
In the second part, the finite difference time domain method FDTD is used to simulate the transmission spectrum for different values of refractive index.



**Fig.2. Variation of the TM photonic band gap with refractive index for  $r/a=0.36$ .**

Figure 3 reports the simulations for three values of refractive index:  $n=1.51$ ,  $n=1.54$  and  $n=1.57$ . The results show that the largest band gap was found around telecommunications wavelength  $1.55\mu\text{m}$ , it extends from  $\lambda_{\min}=1.510\mu\text{m}$  to  $\lambda_{\max}=1.604\mu\text{m}$ . In the other hand, we have found that more refractive index increases the band gaps shifts towards the higher wavelengths, and the midium wavelength  $\lambda_0=(\lambda_{\min}+\lambda_{\max})/2$  varied from  $\lambda_0=1.521\mu\text{m}$  to  $\lambda_0=1.557\mu\text{m}$ .

Finally, we can conclude that the increasing of refractive index from 1.51 to 1.57 induced more increasing in the width. Consequently, the refractive index was fixed at 1.57 for different transmission spectrum simulations in the following sections.

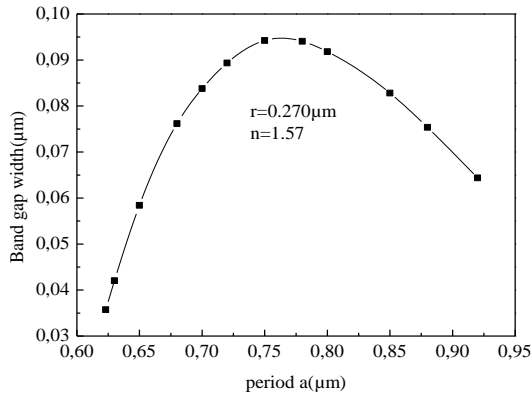


**Fig.3. Transmittance versus wavelength for different value of index of 2D photonic crystal for  $r/a=0.36$ .**

## III. Effect of lattice period

In the following section, we consider the structure described in figure 1 which is formed by  $33 \times 33$  triangular array, the air hole radius was fixed at  $r=0.27\mu\text{m}$  and the background index used in all simulations is  $n=1.57$ . Then we simulate the transmission spectrum for different lattice periods.

Figure 4 reports the variations of the photonic band gap width as a function of the lattice period  $a$ .

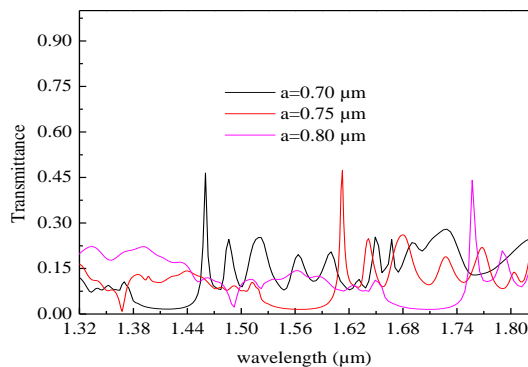


**Fig.4. Band gap width as a function of lattice period of 2D photonic crystal for  $n=1.57$  and  $r=0.27\mu\text{m}$ .**

From results we can observe that the band gap was opened from  $a=0.623\mu\text{m}$  and disappears from  $a=0.92\mu\text{m}$ , between the two values of period the size of photonic band gap was varying like as a Gaussian function with lattice period  $a$ . In the other hand, the bandwidth is maximum for  $a=0.75\mu\text{m}$  ( $\Delta\lambda=0.0942\mu\text{m}$ ) and the photonic band gap extends from  $\lambda_{\min}=1.510\mu\text{m}$  to  $\lambda_{\max}=1.604\mu\text{m}$  (Figure 3 for  $n=1.57$ ).

Figure 5, shows the results of transmission spectrum simulated by finite difference time domain method (FDTD) in Fullwave of TM mode for three values of period:  $a=0.7\mu\text{m}$ ,  $a=0.75\mu\text{m}$  and  $a=0.8\mu\text{m}$ .

The results demonstrate clearly that more the lattice period increases, the photonic band gap shifts towards the higher wavelengths, and the medium wavelength  $\lambda_0=(\lambda_{\min}+\lambda_{\max})/2$  increases from  $\lambda_0=0.078\mu\text{m}$  for  $a=0.7\mu\text{m}$  to  $\lambda_0=0.0918\mu\text{m}$  for  $a=0.8\mu\text{m}$ .

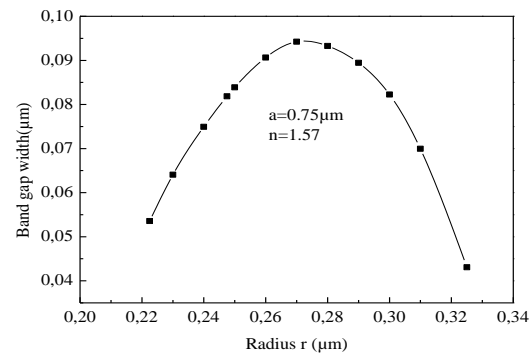


**Fig.5. Transmittance versus wavelength for different value of lattice period of 2D photonic crystal for  $n=1.57$  and  $r=0.27\mu\text{m}$ .**

#### IV. Effect of air hole radius

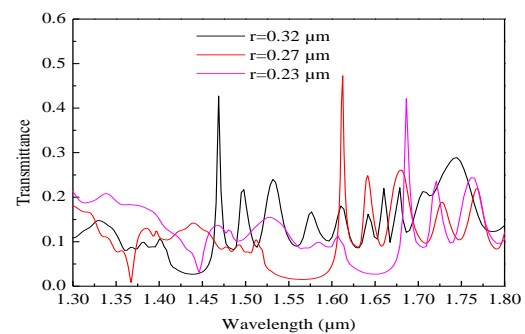
In order to study and analyze the effect of air hole radius on the variations of photonic band gaps of 2D photonic crystals characterized with low contrast and structured in triangular lattice, we consider the structure shown in figure 1 which is characterized with a lattice constant  $a=0.75\mu\text{m}$  and a refractive index  $n=1.57$ . After that, a series of simulations of spectrum transmission for different values of radius from  $r=0.223\mu\text{m}$  to  $r=0.325\mu\text{m}$  were carried, then we calculate the band gap width for each radius. The results show that photonic band gap exists only for TM polarization (transverse magnetic), the band gap width is maximum for  $r=0.27\mu\text{m}$  ( $r/a=0.36$ ).

In figure 6, we have reported the variations of the bandwidth as a function of air hole radius for a lattice period  $a=0.75\mu\text{m}$  and a refractive index equal 1.57.



**Fig.6. Band gap width as a function of air hole radius of 2D photonic crystal for  $n=1.57$  and  $a=0.75\mu\text{m}$ .**

The simulation of the transmission spectrum by finite difference time domain method (FDTD) of TM mode (transverse magnetic) for three values of radius  $r=0.23\mu\text{m}$ ,  $r=0.27\mu\text{m}$  and  $r=0.32\mu\text{m}$  were reported in figure 7. They occur that more radius increase the photonic band gaps shift towards the lower wavelengths where the medium wavelength  $\lambda_0$  varied from  $\lambda_0=1.645\mu\text{m}$  for  $r=0.23\mu\text{m}$  to  $\lambda_0=1.436\mu\text{m}$  for  $r=0.32\mu\text{m}$ .



**Fig.7. Transmittance versus wavelength for different value of air hole radius of 2D photonic crystal for  $n=1.57$  and  $a=0.75\mu\text{m}$ .**

## V. Conclusion

Photonic band gap of two dimensional photonic crystals made with  $\text{SiO}_2 / \text{ZrO}_2$  or  $\text{SiO}_2 / \text{TiO}_2$  and characterized by low refractive index which change in the range of 1.51 to 1.57 have been investigated and reported in the present paper. The different results of simulation obtained by FDTD method in Fullwave software are clearly demonstrated the existence of the photonic band gap of triangular lattice structure which formed by air holes embedded in matrix. Firstly, the results show that the refractive index has a great effect on photonic band gap width. Furthermore, the results show that the geometric parameters (air hole radius "r" and lattice period "a") have a great influence on the position and the width of photonic band gap. In the other hand, the PBG exist only for radius r varied in the range of  $0.223\mu\text{m}$  to  $0.325\mu\text{m}$  and for period a change in range of  $0.623\mu\text{m}$  to  $0.92\mu\text{m}$ . Thus we reveal that a maximum absolute band gap for this structure is achieved for  $n=1.57$ ,  $a=0.75\mu\text{m}$  and  $r=0.27\mu\text{m}$ .

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